# FOOD PROCESSING & PRESERVATION, INFORMATION &

## COMMUNICATION, INSTRUMENT, INSTRUMENTATION, MECHATRONICS AND TELECOMMUNICATION TECHNOLOGIES.

## MATH.123 APPLIED MATHEMATICS-I

# PAPER 'B' (Subjective)

Time: 2:30 Hours

Marks: 60

### SECTION-I

Write short answers to any Eighteen (18) from the following questions.

18x2 = 36

- Write the conjugate and modulus of  $-\frac{2}{3} \frac{4}{9}i$
- Prove that if  $Z = \overline{Z}$ , then  $\overline{Z}$  is real. Factorize  $2x^2 + 5y^2$
- 3.
- Express complex number  $3-\sqrt{3}i$  in polar (trigonometric) form. 4.
- Express |Z| = 3 and  $\arg Z = -\frac{\pi}{2}$  in the form x + iy5.
- Define improper fraction and given one example:
- Resolve  $\frac{1}{x^2-1}$  into partial fraction:
- Write an identity equation of  $\frac{2x+5}{x^2+5x+6}$
- Form of partial fraction of  $\frac{1}{(x+1)^2(x-2)}$  is \_\_\_\_
  - Define "Binary Number". 10.
  - Convert octal number 1078 to binary numbers. 11.
  - Prove  $X + X \neq X = X$  by Boolean Algebra rules. 12.
  - 13. Prove  $X(\overline{X} + Y) = XY$  by Boolean Algebra rules.
  - 14. Prepare a truth table of X(X + Y) = X
  - Find the co-ordinate of the mid-point of the segment  $P_1$  (3,7),  $P_2$  (-2, 3). 15.
  - For the triangle whose vertices are A(0,1), B (7,2) and C(3,8). Find the length of the 16. median from C to AB.
  - Find the angle between the lines having slopes -3 and 2 17:
  - Find the equation of a line through the point (3,-2) with slope  $m = \frac{3}{4}$ . 18.
  - Find the equation of a line whose perpendicular distance from the origin is 2, and 19. inclination of the perpendicular is 225°.
  - Find the equation of the line passing the point (1, -2) making an angle of 135° with 20. the x-axis.
  - Find the point of intersection of the lines x + 2y 3 = 0, 2x 3y + 8 = 021.
  - Show that the points (1,9), (-2,3) and (-5,-3) are collinear. 22.
  - Show that the lines passing through the points (0, -7), (8, -5) and (5, 7), (8, -5) are 23. perpendicular.
  - Write the equation of circle with centre at (h, k) and radius r. 24.
  - Find centre and radius of the circle  $x^2 + y^2 + 9x 7y 33 = 0$ 25.
  - Reduce the equation into standard form  $\dot{x}^2 + y^2 4\dot{x} + 6y 12 = 0$ 26.
  - Find the equation of the circle which touches both the axes of 4th quadrant and 27. has a radius of 5 units.

### SECTION-II

Note: Attempt any three (03) questions.

3x8 = 24

- Q. 2 (a) Extract the square root of -3 + 4i.
- (b) Write complex number 4 Cis 240° in the form a + bi.
- Q. 3 Resolve  $\frac{1}{(1-x)(1-2x)(1-3x)}$  into partial fraction.
  - (b) Resolve  $\frac{1}{x^3 1}$  into partial fraction.
- Q. 4(a) Convert  $18 \times 24$  to binary form and then perform binary multiplication.
  - (b) Minimize the expression  $X = \overline{A} B \overline{C} + A \overline{B} \overline{C} + \overline{A} \overline{B} \overline{C} + \overline{A} \overline{B} \overline{C}$
- Q. 5 (a) The point (x, y) is on the x-axis and is 6 units away from the point (1, 4), find x and y.
  - (b) Find the points trisecting the join of A(-1, 4) and B(6, 2)
- Q. 6 Find the equation of the circle Passing through the points (0,1), (3,-3) and (3,-1).

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