

**DAE/IA – 2017/02      SECOND YEAR**

(Common with Architecture, Automation, Auto-Mobile & Diesel,  
Auto & Farm Machinery, Civil, Cast Metal & Foundry,  
Foundry & Pattern Making, Land & Mine Surveying, Mechanical,  
Mining, Mechatronics, Metallurgy & Welding, Q. Surveying ,  
Construction Machinery and Footwear Technologies)

**MATH – 212 APPLIED MATHEMATICS - II**

**PART – B**

Time: 2:30 hours

Marks: 80

**SECTION - I**

**Q.1 Write short answers to any Twenty Five (25) of the following questions:-**

**25 x 2 = 50**

1.	If $f(x) = 3x^2 - 5x + 7$ , find $f(4)$	2.	Is the following function even, odd or neither? $f(x) = 4x^3 - 2x + 6$
3.	Evaluate $\lim_{x \rightarrow 1} \frac{x^2 - 1}{x - 1}$	4.	Evaluate $\lim_{x \rightarrow 0} \frac{1 - \cos 2x}{x^2}$
5.	Differentiate $\frac{1}{5}x^{\frac{5}{2}} + \frac{1}{3}x^{\frac{3}{2}}$ w.r.t 'x'	6.	Differentiate $\sqrt{x^2 + 1}$ w.r.t 'x'
7.	Differentiate $\sin(\tan x)$ w.r.t 'x'	8.	Find $\frac{dy}{dx}$ if $x^{\frac{2}{3}} + y^{\frac{2}{3}} = a^{\frac{2}{3}}$
9.	Differentiate $2x^2 + x + 1$ w.r.t $x^2 - x - 1$	10.	Differentiate $\tan^{-1} \sqrt{x}$ w.r.t 'x'
11.	Differentiate $x \ln x - x$ w.r.t 'x'	12.	Differentiate $e^{\sin 2x}$ w.r.t 'x'
13.	Differentiate $\sin x$ w.r.t $\tan x$ .	14.	If $x = \sin 2t$ , $y = 2 \cos t$ then find $\frac{dy}{dx}$
15.	Find derivative of $x\sqrt{x+1}$ w.r.t 'x'	16.	Find the critical values (turning points) for x of the function $x^2 - 4x - 1$
17.	Evaluate $\int \left( \sqrt{x} + \frac{1}{\sqrt{x}} \right) dx$	18.	Evaluate $\int \frac{1}{2} \left( e^{\frac{1}{2}x} - e^{-\frac{1}{2}x} \right) dx$
19.	Evaluate $\int \cot^2 x dx$	20.	Evaluate $\int \frac{x^2 + 1}{x + 1} dx$
21.	Evaluate $\int \sqrt{\sin x} \cos x dx$	22.	Evaluate $\int \frac{dx}{(1+x^2)\tan^{-1}x}$
23.	Evaluate $\int \frac{\ln x}{x} dx$	24.	Evaluate $\int x \cos 3x dx$
25.	Evaluate $\int_1^8 \frac{dx}{\sqrt[3]{x}}$	26.	Evaluate $\int_0^{\frac{\pi}{6}} \sec^2 x dx$
27.	Evaluate $\int \frac{x^3 + 1}{x^5} dx$	28.	Find the distance between (-4, 2) and (0, 5)
29.	Show that the points (2, 6), (-8, 1) and (-2, 4) are collinear.	30.	Find the equation of a line through the point (3, -2) with slope $m = \frac{3}{4}$
31.	Reduce the equation $3x + 4y - 2 = 0$ into intercept form.	32.	Find the slope of a line which is perpendicular to the line joining $P_1(2, 4), P_2(-2, 1)$
33.	Is the point (0, 4) inside or outside the circle of radius 4 with center at (-3, 1).	34.	For the triangle $A(1, 3), B(-2, 1), C(0, -4)$ find slope of a line parallel to AC.
35.	Find the equation of the circle with the given center and radius (-1, 2), $r = \sqrt{2}$	36.	Find the center and radius of the circle $X^2 + y^2 - 4x + 6y - 12 = 0$
37.	Write the general form of the circle, also represent the center and radius in this form.		

SECTION - II

NOTE: ATTEMPT ANY THREE QUESTIONS.

3 x 10 = 30

- Q.2 a) If  $f(x) = \frac{x-1}{x+1}$ , show that  $\frac{f(x)-f(y)}{1+f(x)f(y)} = \frac{x-y}{1+xy}$   
b) Differentiate  $\left(\frac{x+1}{x-1}\right)^2$  w.r.t 'x' (5,5)
- Q.3 a) Find the derivative of  $\frac{\sin x}{1-\cos x}$  w.r.t 'x'  
b) Find the maximum and minimum (extreme) values of the function  $(x-2)^2(x-1)$  (5,5)
- Q.4 a) Evaluate  $\int \frac{dx}{\sqrt{x+a}+\sqrt{x+b}}$   
b) Evaluate  $\int \sin^3 x \, dx$  (5,5)
- Q.5 a) Integrate  $\int x^2 \tan^{-1} x \, dx$   
b) Find the point which is two third of the way from the point (5,1) to the point (-2,9). (5,5)
- Q.6 a) Show that the given points are the vertices of a parallelogram (-3,1), (-1,7), (2,8) and (0,2)  
b) Find the equation of circle having (-2,5) and (3,4) as the end points of its diameter. Find also its center and radius. (5,5)
- =====