

TAHIR
M.Sc. (Math)

Exercise 1.5

Q.1 Draw the Graph of the following equations :

(i) $x^2 + y^2 = 9 \Rightarrow y^2 = 9 - x^2 \Rightarrow y = \pm\sqrt{9 - x^2}$

x	-3	-2	-1	0	1	2	3
y	0	± 2.24	± 2.83	± 3	± 2.83	± 2.24	0
(x,y)	(-3,0)	(-2, 2.24) (-2, -2.24)	(-1, 2.83) (-1, -2.83)	(0, 3) (0, -3)	(1, 2.83) (1, -2.83)	(2, 2.24) (2, -2.24)	(3, 0)

(ii) $\frac{x^2}{16} + \frac{y^2}{4} = 1 \Rightarrow x^2 + 4y^2 = 16 \Rightarrow 4y^2 = 16 - x^2$
 $\Rightarrow y^2 = \frac{16 - x^2}{4} \Rightarrow y = \pm \frac{\sqrt{16 - x^2}}{2}$

x	-4	-3	-2	-1	0	1	2	3	4
y	0	± 1.32	± 1.73	± 1.94	± 2	± 1.94	± 1.73	± 1.32	0
(x,y)	(-4,0)	(-3, 1.32) (-3, -1.32)	(-2, 1.73) (-2, -1.73)	(-1, 1.94) (-1, -1.94)	(0, 2) (0, -2)	(1, 1.94) (1, -1.94)	(2, 1.73) (2, -1.73)	(3, 1.32) (3, -1.32)	(4, 0)

(iii) $y = e^{2x} \Rightarrow e \approx 2.71$

x	-1.5	-1	-0.5	0	0.5	1	1.5
y	0.22	0.37	0.61	1	1.65	2.71	4.5
(x,y)	(-1.5, 0.22)	(-1, 0.37)	(-0.5, 0.61)	(0, 1)	(0.5, 1.65)	(1, 2.71)	(1.5, 4.5)

(iv) $y = 3^x$

x	-1.5	-1	-0.5	0	0.5	1	1.5
y	0.19	0.33	0.58	1	1.73	3	5.2
(x,y)	(-1.5, 0.19)	(-1, 0.33)	(-0.5, 0.58)	(0, 1)	(0.5, 1.73)	(1, 3)	(1.5, 5.2)

Q.2 Graph the following parametric curves equations:

(i) $x = t$, $y = t^2$ $-3 \leq t \leq 3$ (t is parameter)

t	-3	-2	-1	0	1	2	3
x	-3	-2	-1	0	1	2	3
y	9	4	1	0	1	4	9

(ii) $x = t - 1$, $y = 2t - 1$ $-1 < t < 5$ (t is parameter)

t	0	1	2	3	4
x	-1	0	1	2	3
y	-1	1	3	5	7

(iii) $x = \sec \theta$, $y = \tan \theta$ (θ is parameter)

θ	-90°	-60°	-30°	0°	30°	60°	90°
x	$+\infty$	2	1.15	1	1.15	2	$+\infty$
y	$-\infty$	-1.73	-0.58	0	0.58	1.73	$+\infty$

Q.3 Draw the graph of the given function and check continuity:

(i) $y = \begin{cases} x-1 & x < 3 \\ 2x+1 & \text{if } x \geq 3 \end{cases}$

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x	0	1	2	3	4	5	6
y	-1	0	1	7	9	11	13

(ii) $y = \frac{x^2 - 4}{x - 2}$, $x \neq 2$

x	-1	0	1	3	4	5	6
y	1	2	3	5	6	7	8

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(iii) $y = \begin{cases} x+3 & \text{if } x \neq 3 \\ 2 & \text{if } x = 3 \end{cases}$

x	0	1	2	3	4	5	6
y	3	4	5	2	7	8	9

(iv) $y = \frac{x^2-16}{x-4}, x \neq 4$

x	1	2	3	5	6	7
y	5	6	7	9	10	11

Q-4 Find the graphical solutions of the following equations:

(i) $x = \sin 2x$

Let $y = x$ and $y = \sin 2x$

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x	-2	-1	0	1	2	3
y=x	-2	-1	0	1	2	3

x	-90°	-60°	-30°	0°	30°	60°	90°
y = sin 2x	0	-0.86	-0.86	0	0.86	0.86	0

(ii) $\frac{x}{2} = \cos x$

Let $y = \frac{x}{2}$ and $y = \cos x$

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x	-2	-1	0	1	2	3
y = x/2	-1	-0.5	0	0.5	1	1.5

x	-90°	-60°	-30°	0°	30°	60°	90°
y = cos x	0	0.5	0.86	1	0.86	0.5	0

(iii) $2x = \tan x$

Let $y = 2x$ and $y = \tan x$

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x	-2	-1	0	1	2	3
y = 2x	-4	-2	0	2	4	6

x	-90°	-60°	-30°	0°	30°	60°	90°
y = tan x	-∞	-1.73	-0.58	0	0.58	1.73	∞

Some Useful Definations:-

Constant Function:-

"The function whose range is a definite and fix number is called constant function."

ie. $y = 3a$ (for any value of x , $y = 3a$)

Exponential Function:-

"The function in which variable appears as an exponent (Power) is called Exponential function."

ie. $y = e^x$ $y = a^x$ where $e \approx 2.7184$
 $a \in \mathbb{N}$

Logarithmic Functions:-

"The function containing the Logarithmic operators are called Logarithmic functions."

ie. $y = \text{Log}_a x$ - Common or Briggs Logarithmic function with $a > 0, a \neq 1$

$y = \ln x$ Natural or Napierian Logarithmic function

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with $e \approx 2.7183$ and $\text{Log}_e x = \ln x$

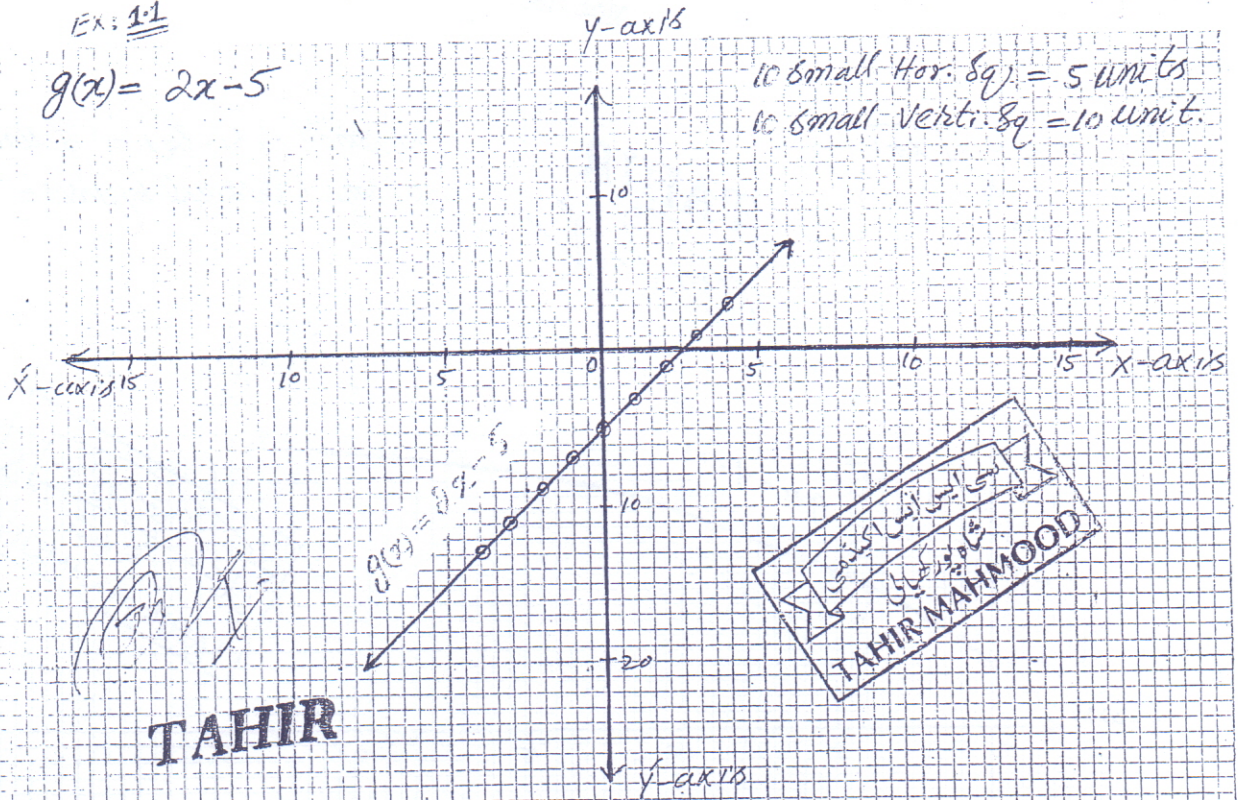
* "Logarithm is an operator which changes a function or term into another equivalent function or term."

$y = \text{Log}_a x \Rightarrow x = a^y$
are equivalent equations having similar value.

Similarly $y = \ln x \Rightarrow x = e^y$

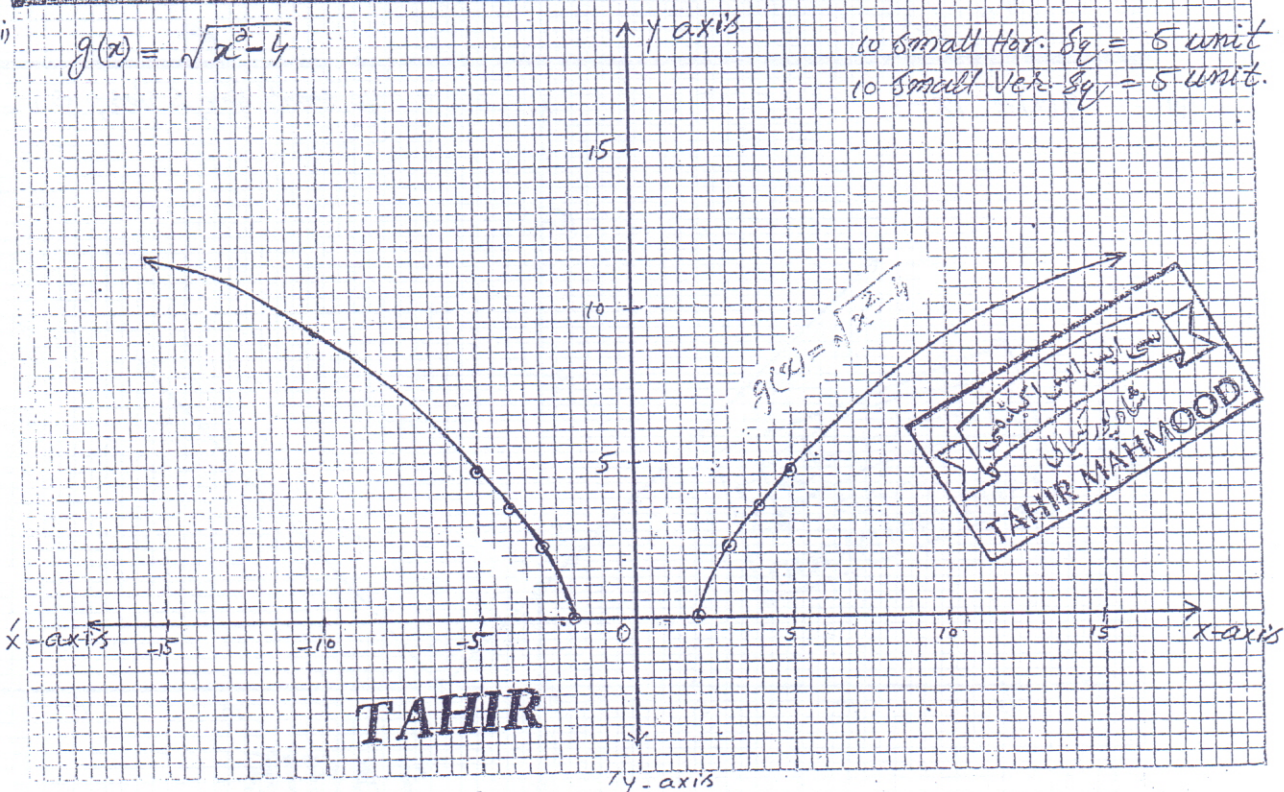
Ex: 1.1

(i) $g(x) = 2x - 5$



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(ii) $g(x) = \sqrt{x^2 - 4}$



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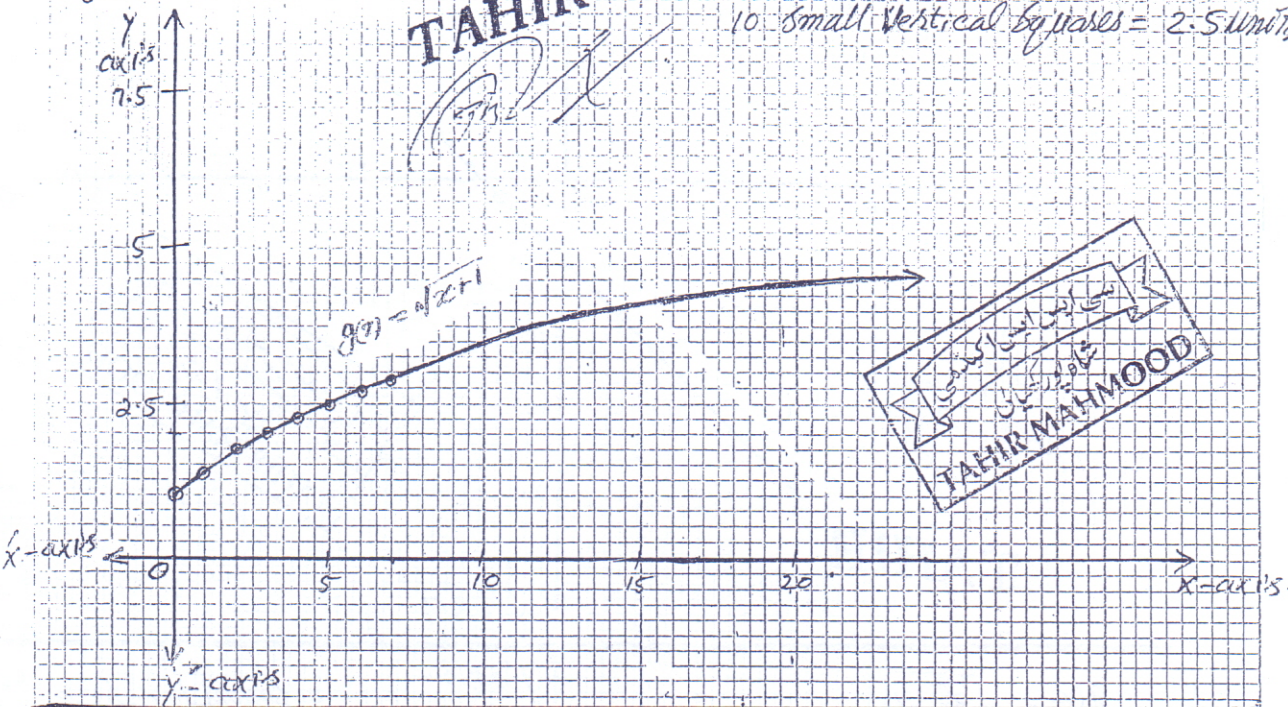
(iii)

$g(x) = \sqrt{x+1}$

10 small Horizontal Segs = 5 units
 10 small Vertical Segs = 2.5 units

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(iv)

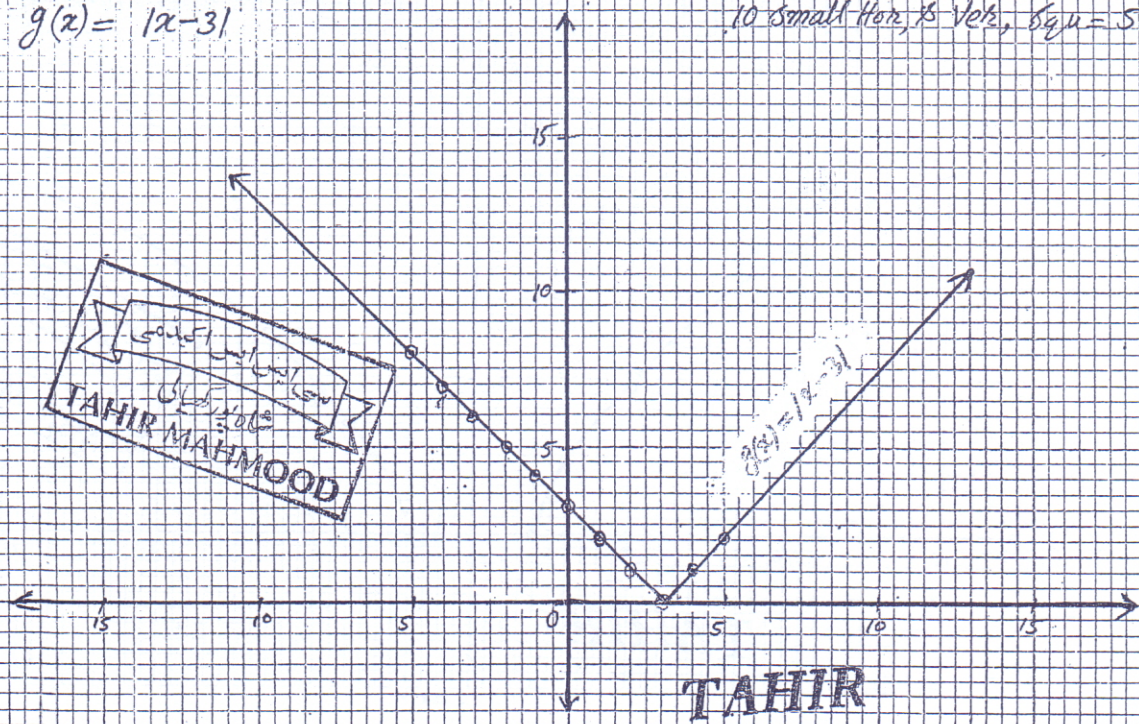
$g(x) = |x-3|$

10 small Horizontal Segs, 10 Vertical Segs = 5 units

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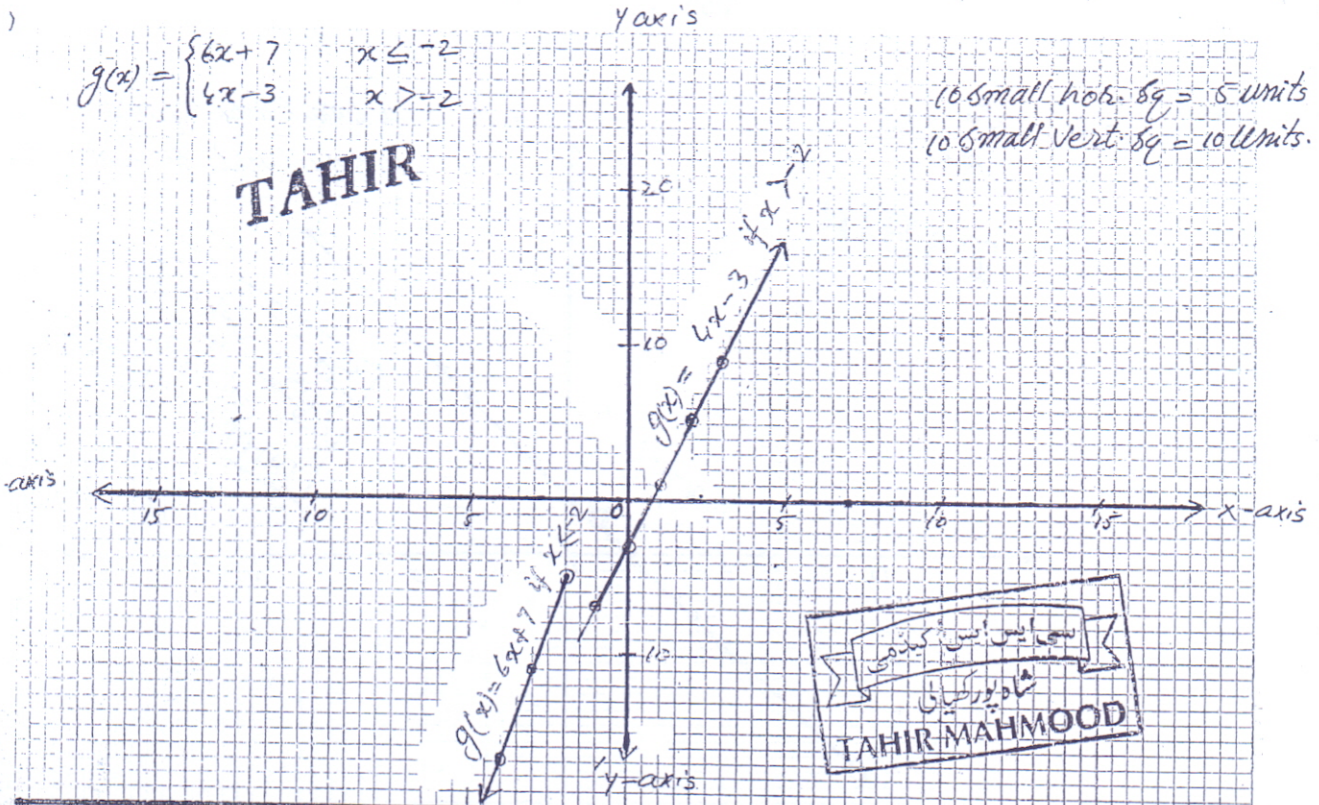
$g(x) = |x-3|$

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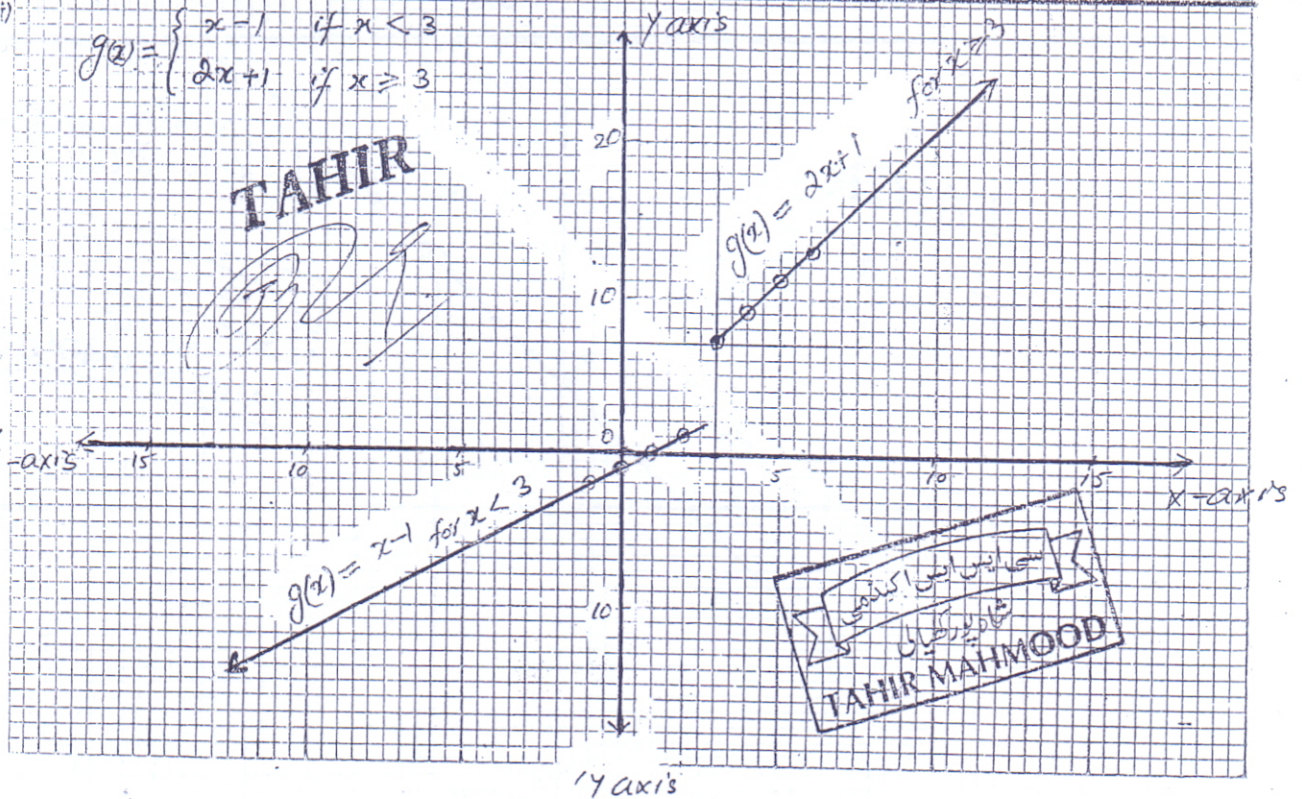
$$g(x) = \begin{cases} 6x+7 & x \leq -2 \\ 4x-3 & x > -2 \end{cases}$$

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$$g(x) = \begin{cases} x-1 & \text{if } x < 3 \\ 2x+1 & \text{if } x \geq 3 \end{cases}$$

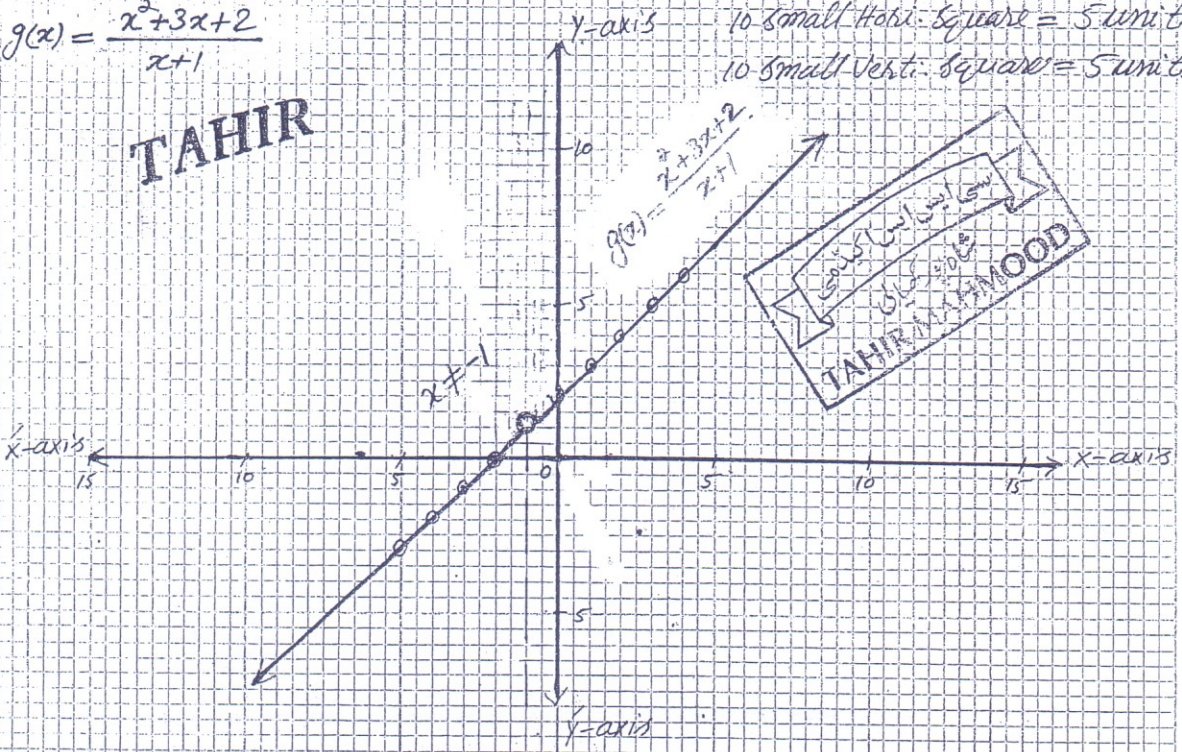
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(vii)

$$g(x) = \frac{x^2 + 3x + 2}{x + 1}$$

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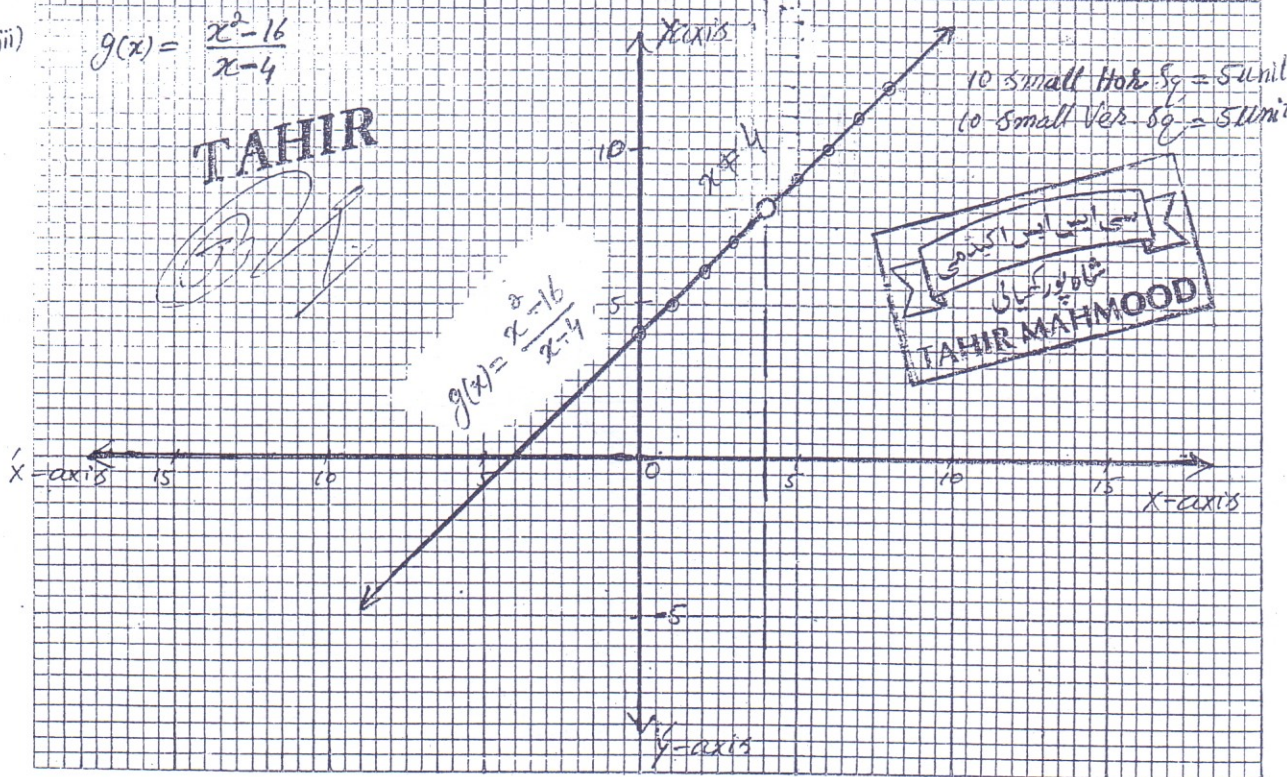


(viii)

$$g(x) = \frac{x^2 - 16}{x - 4}$$

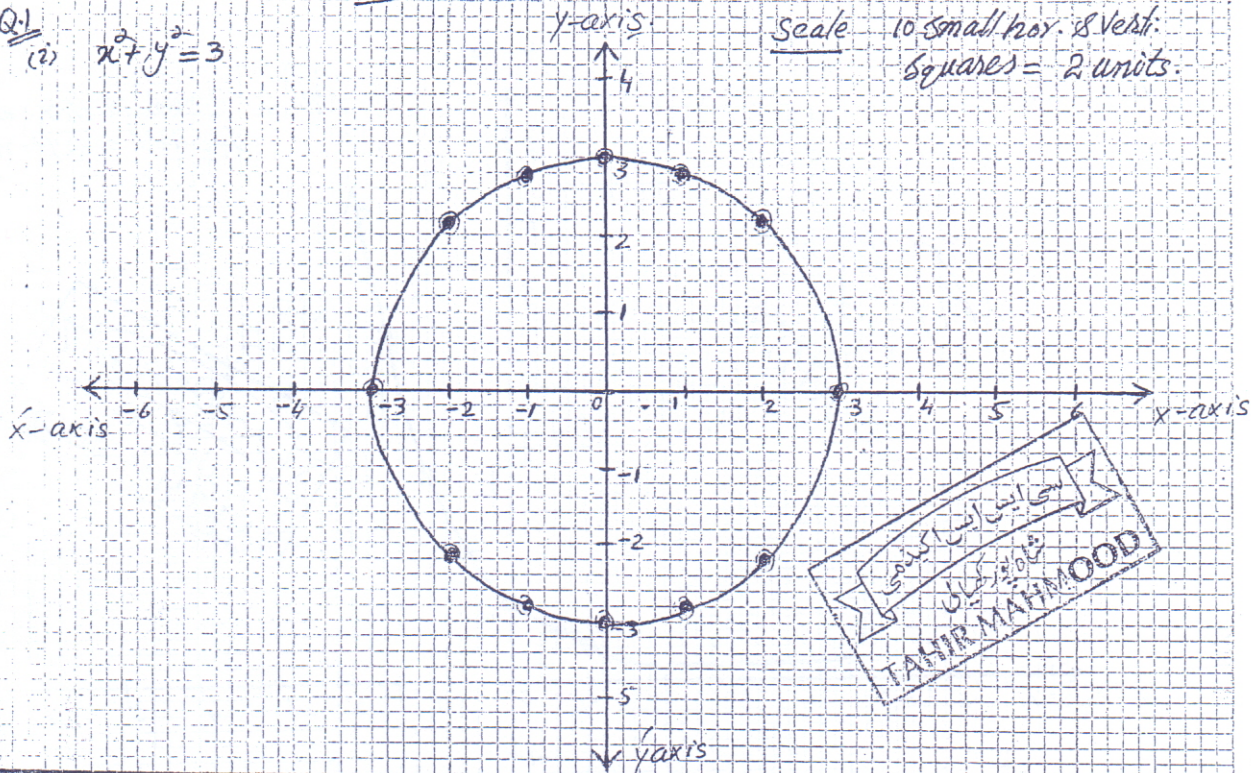
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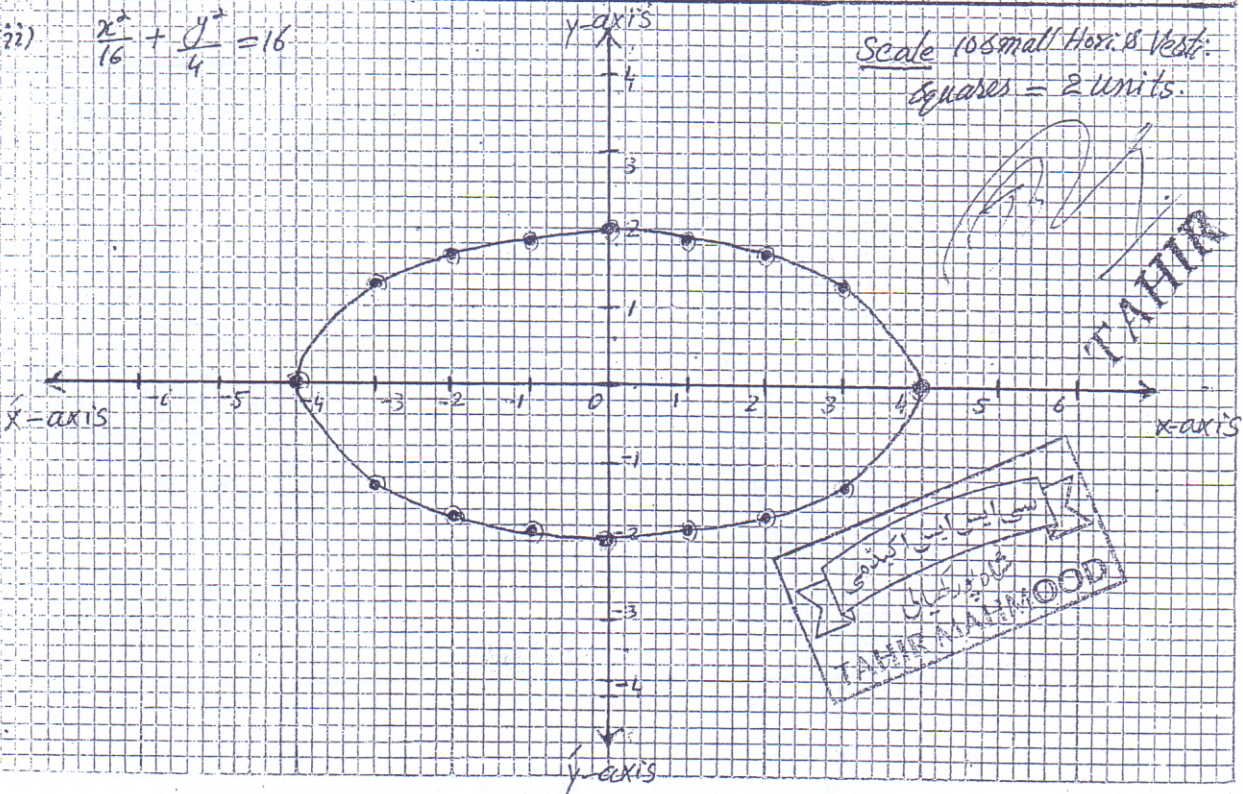


EX. 1.5

Q.1 (i) $x^2 + y^2 = 3$



(ii) $\frac{x^2}{16} + \frac{y^2}{4} = 16$



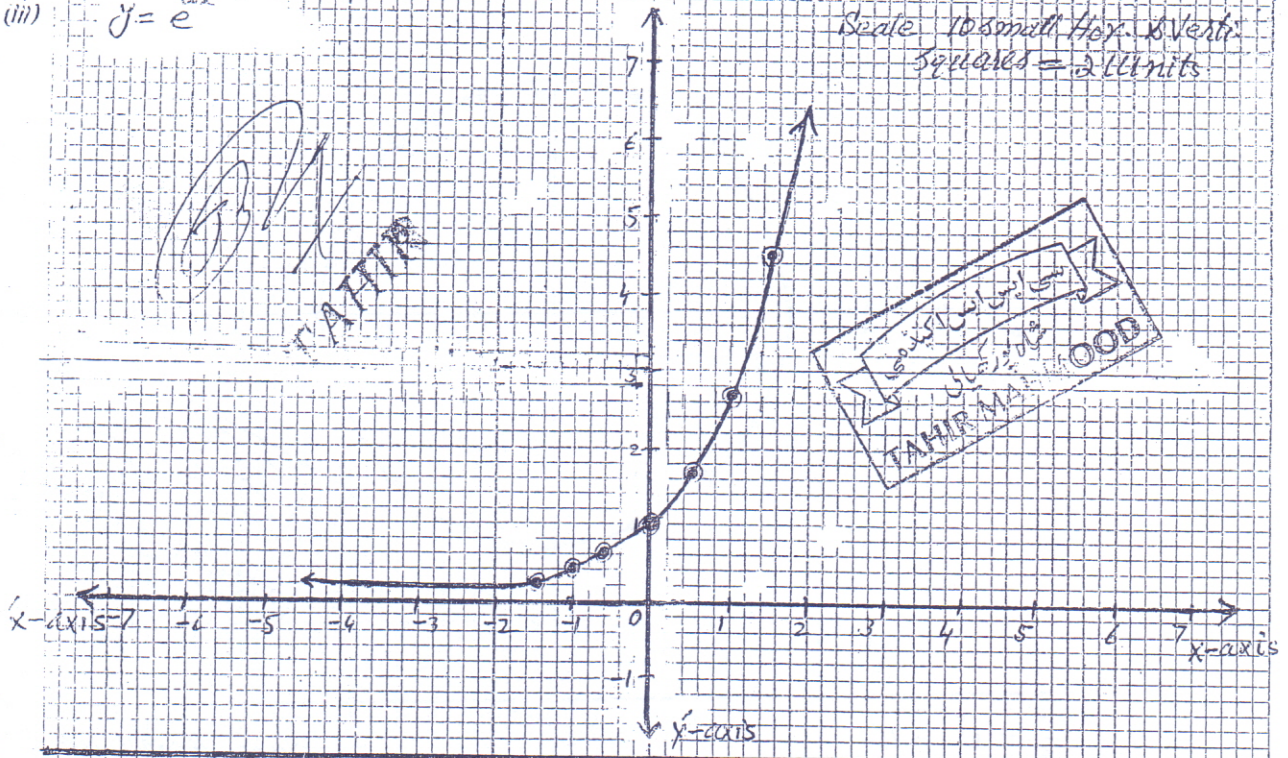
(iii)

$$y = e^{ax}$$

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y-axis

Scale 10 small Hor. & Vert. Squares = 2 Units.

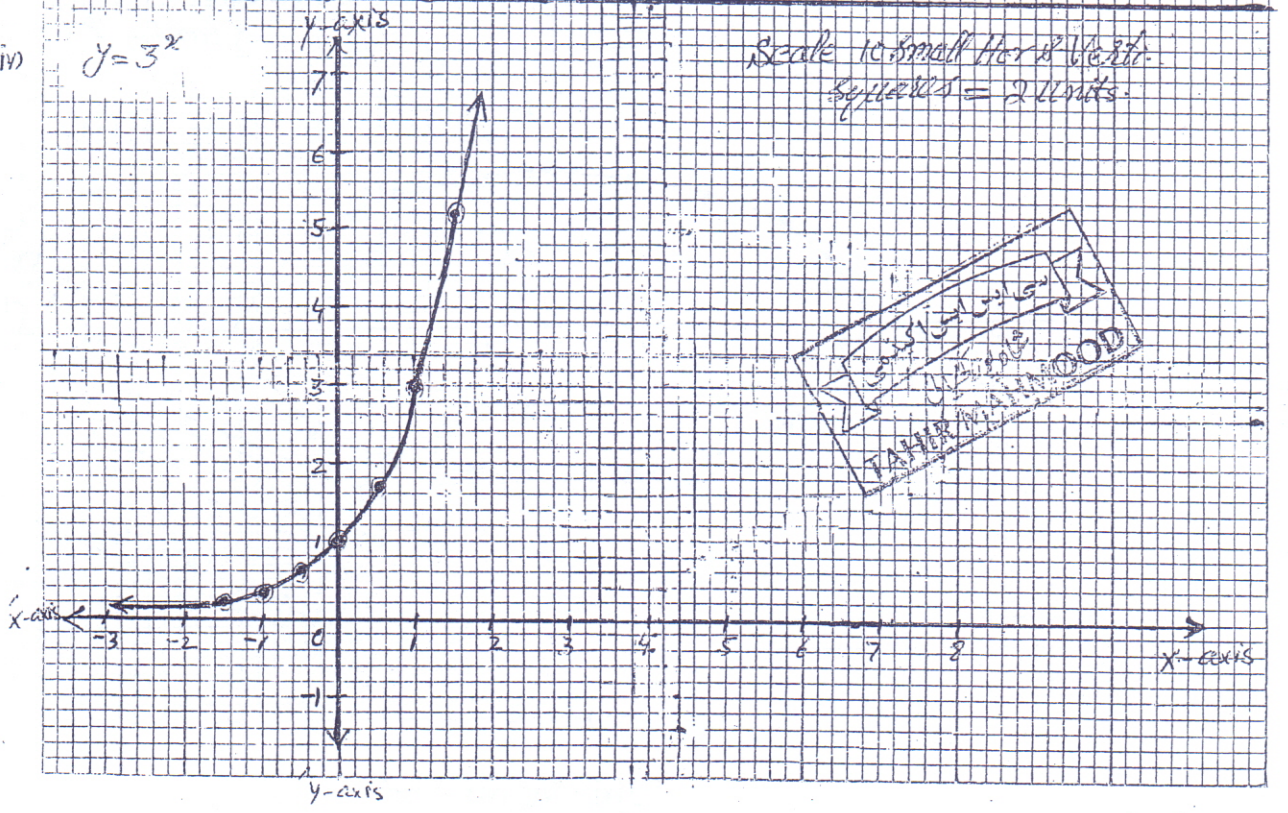


(iv)

$$y = 3^x$$

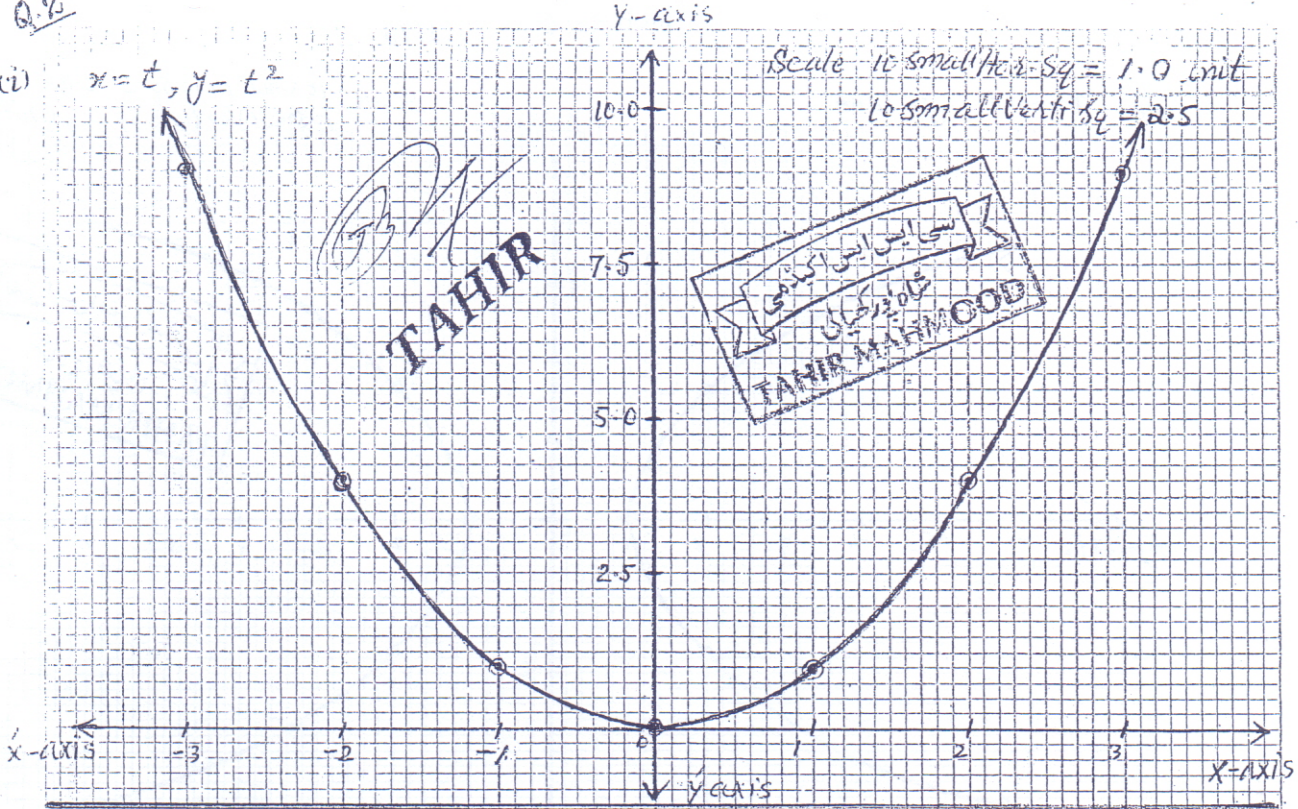
y-axis

Scale 10 small Hor. & Vert. Squares = 2 Units.

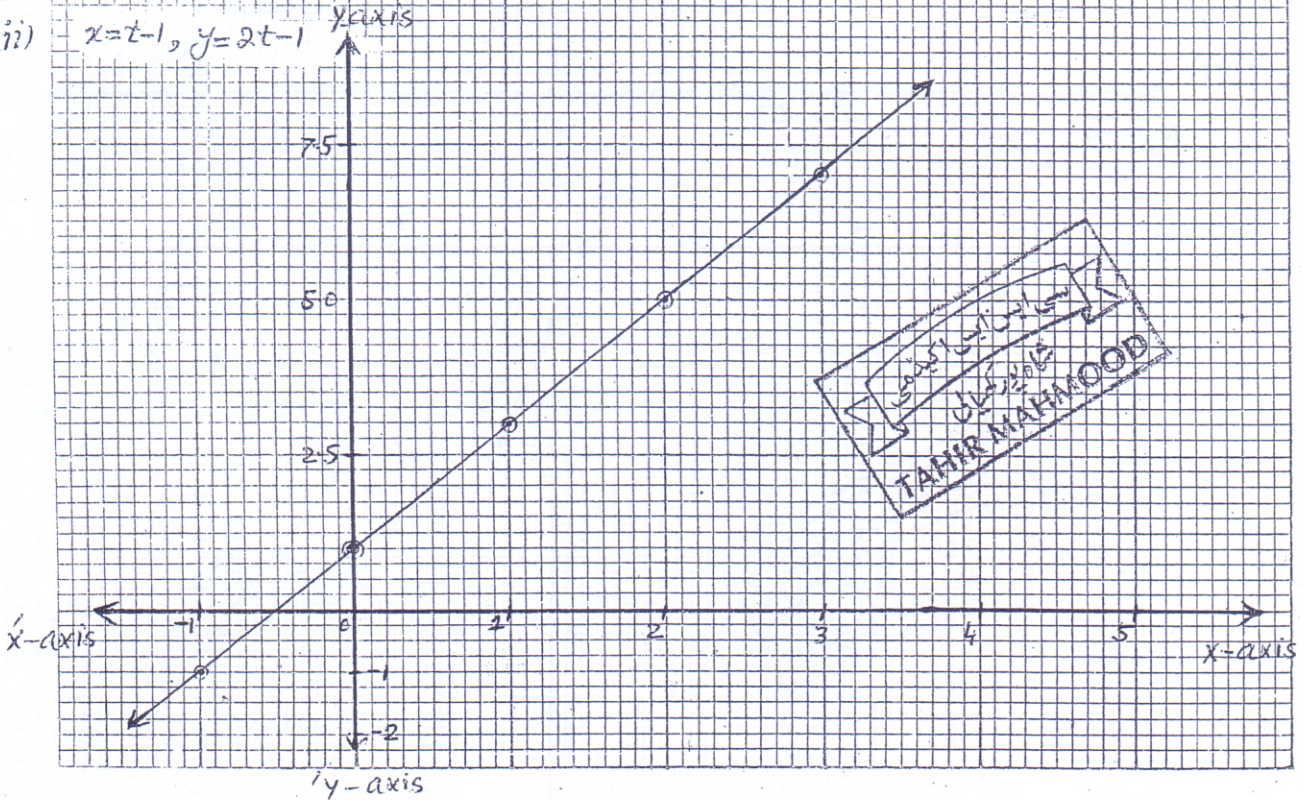


Q.2

(i) $x = t, y = t^2$

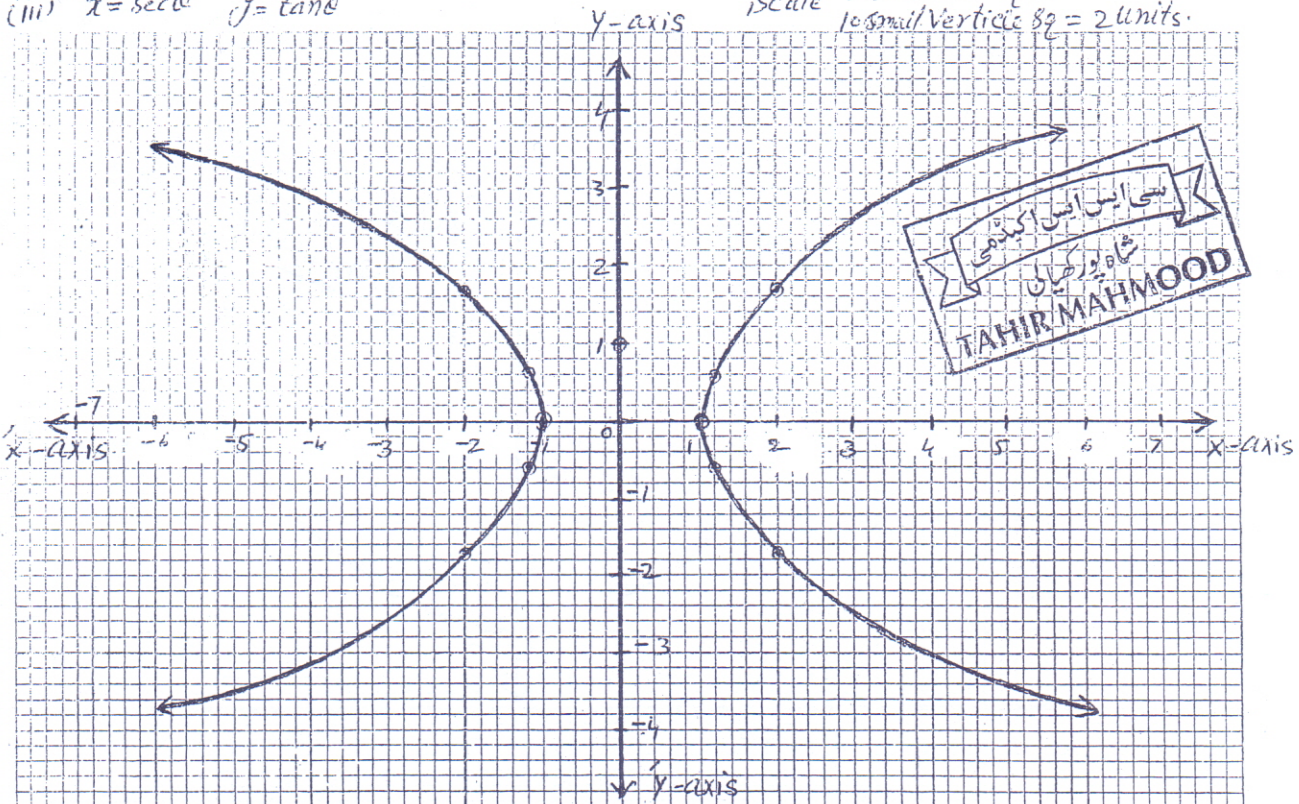


(ii) $x = t-1, y = 2t-1$

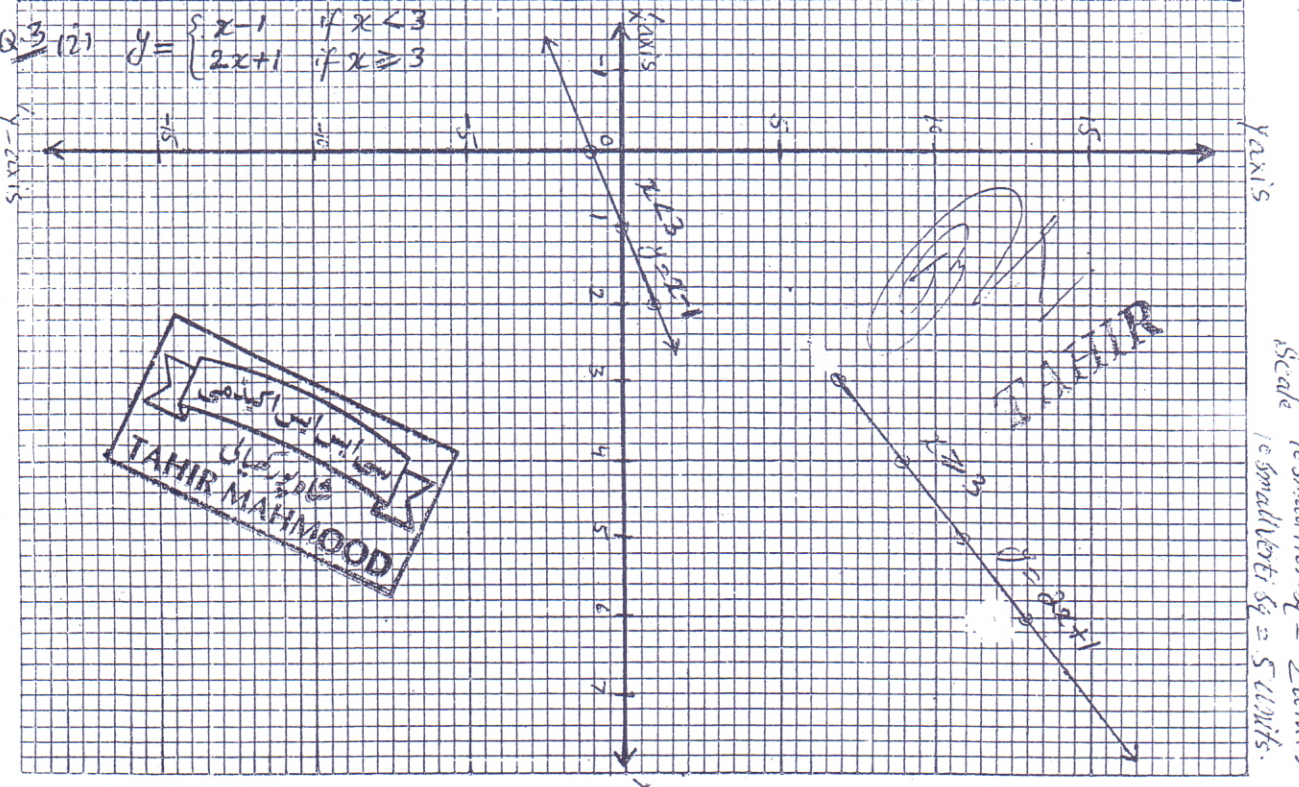


(iii) $x = \sec \theta$ $y = \tan \theta$

Scale 10 small Hor. Sq = 2 units
 10 small Vertice Sq = 2 units.



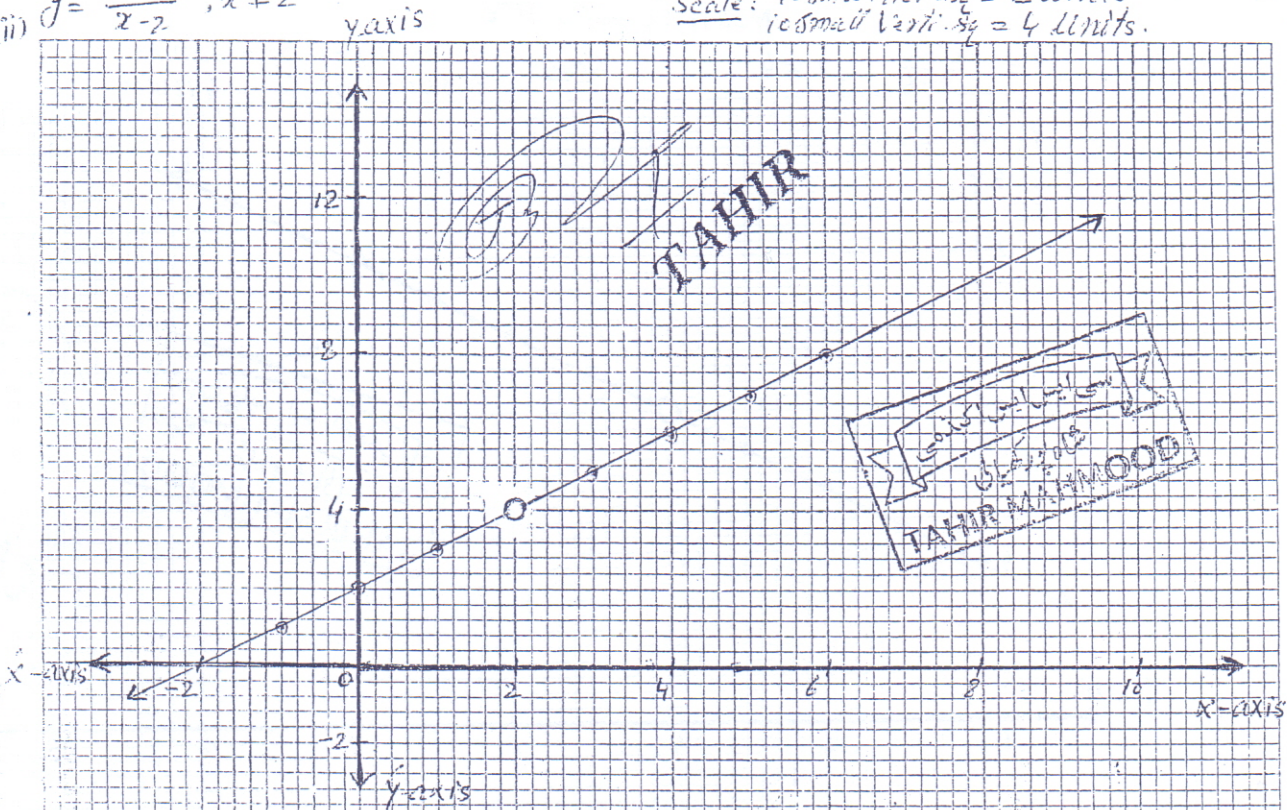
Q.3 (2) $y = \begin{cases} x-1 & \text{if } x < 3 \\ 2x+1 & \text{if } x \geq 3 \end{cases}$



Scale 10 small Hor. Sq = 2 units
 10 small Vertice Sq = 5 units.

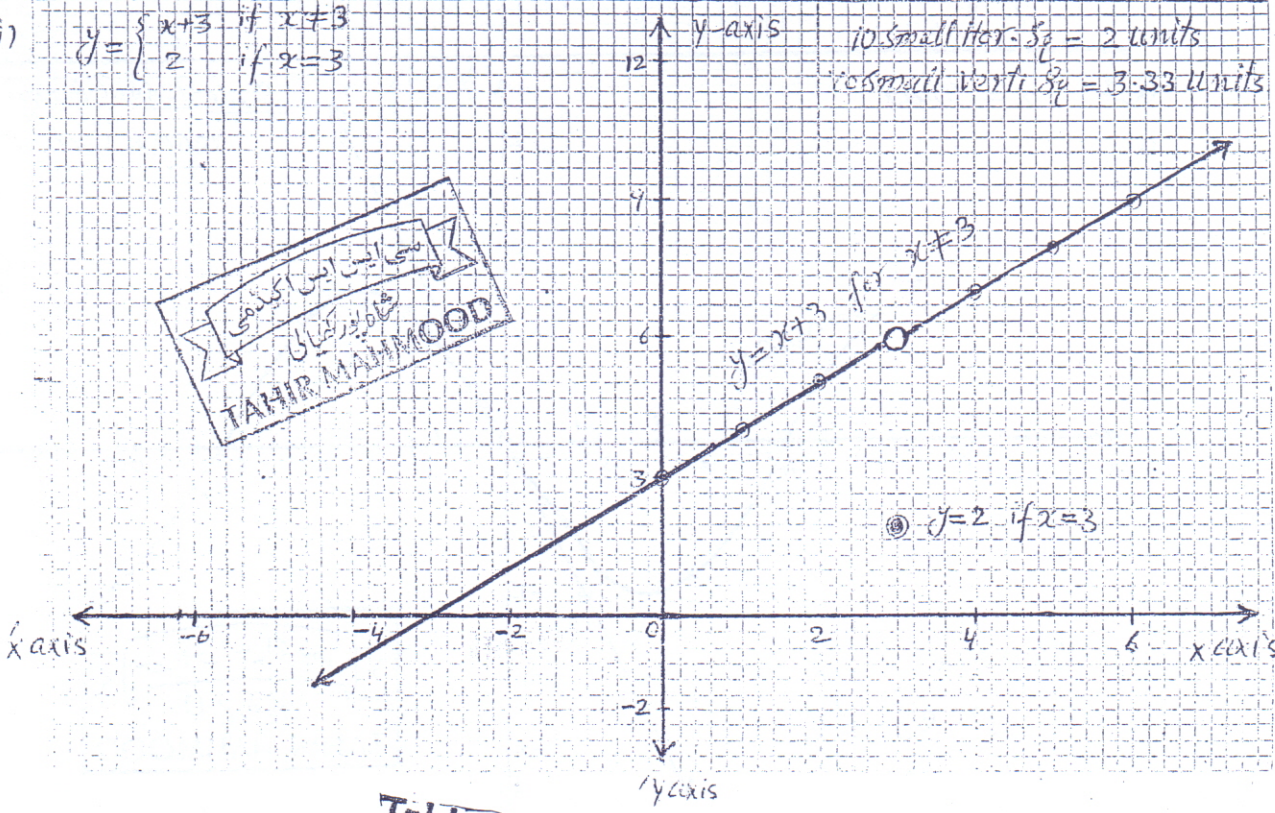
(ii) $y = \frac{x^2 - 4}{x - 2}, x \neq 2$

Scale: 10 small Hor. Sq = 2 units
10 small Verti. Sq = 4 units.



(iii) $y = \begin{cases} x+3 & \text{if } x \neq 3 \\ 2 & \text{if } x = 3 \end{cases}$

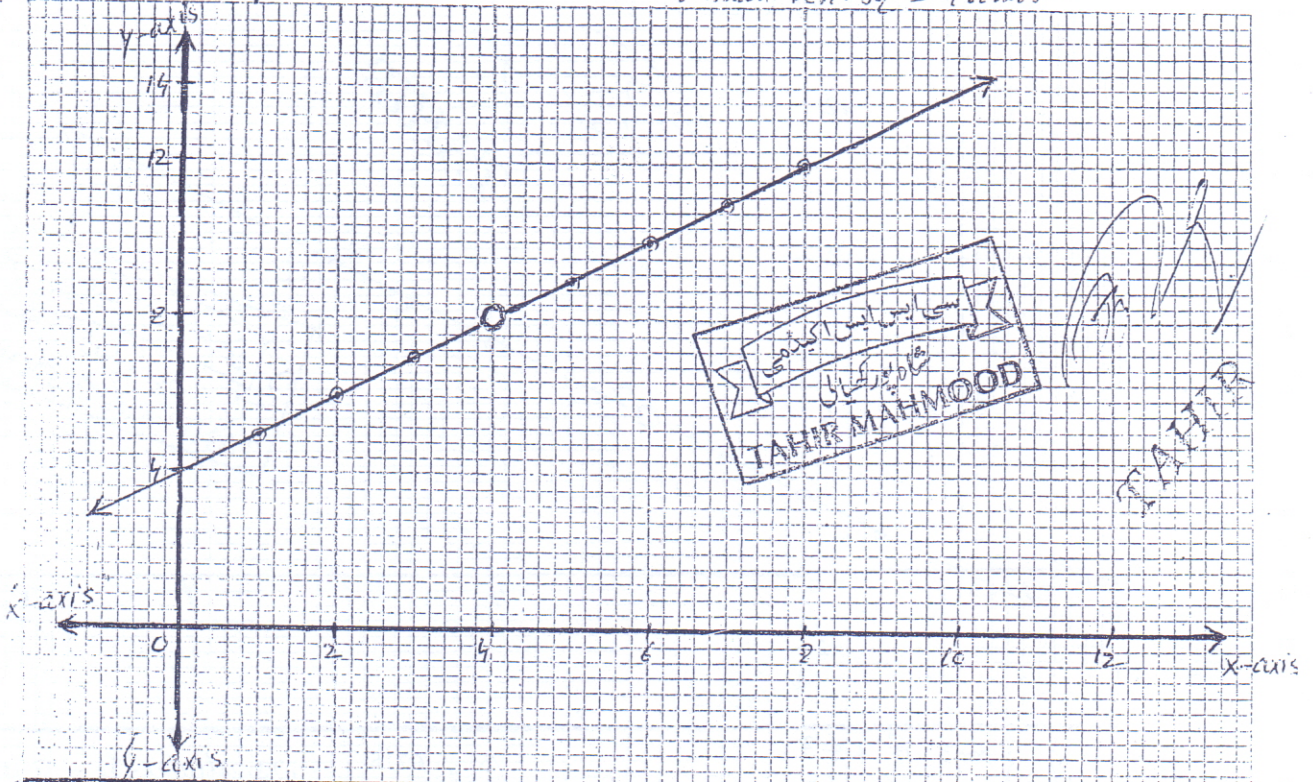
10 small Hor. Sq = 2 units
10 small Verti. Sq = 3.33 units



(iv)

$y = \frac{x^2 - 16}{x - 4}, x \neq 4$

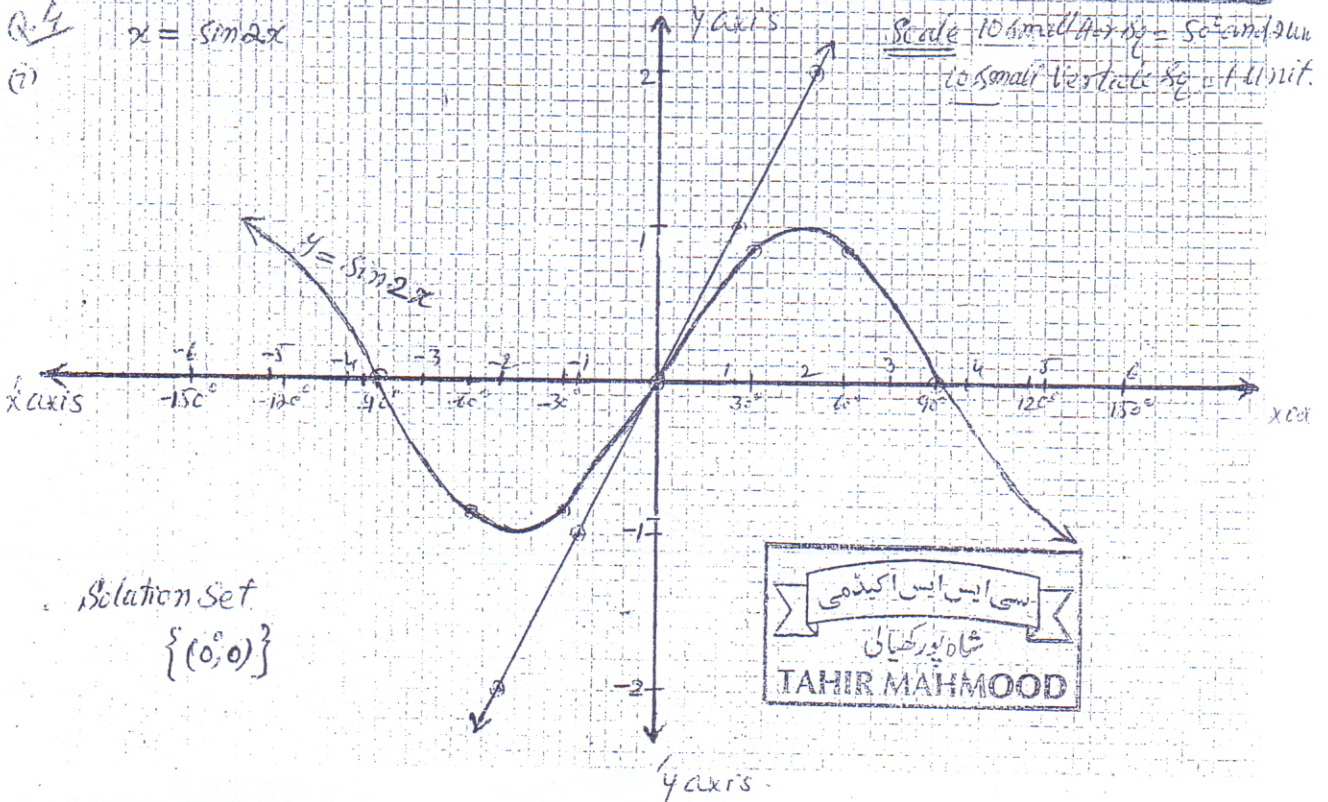
Scale 10 Small Hor. Sq = 2 units
10 Small Vert. Sq = 4 units



Q.4 $x = \sin 2x$

(i)

Scale 10 Small Hor. Sq = 5 units
10 Small Vert. Sq = 1 unit

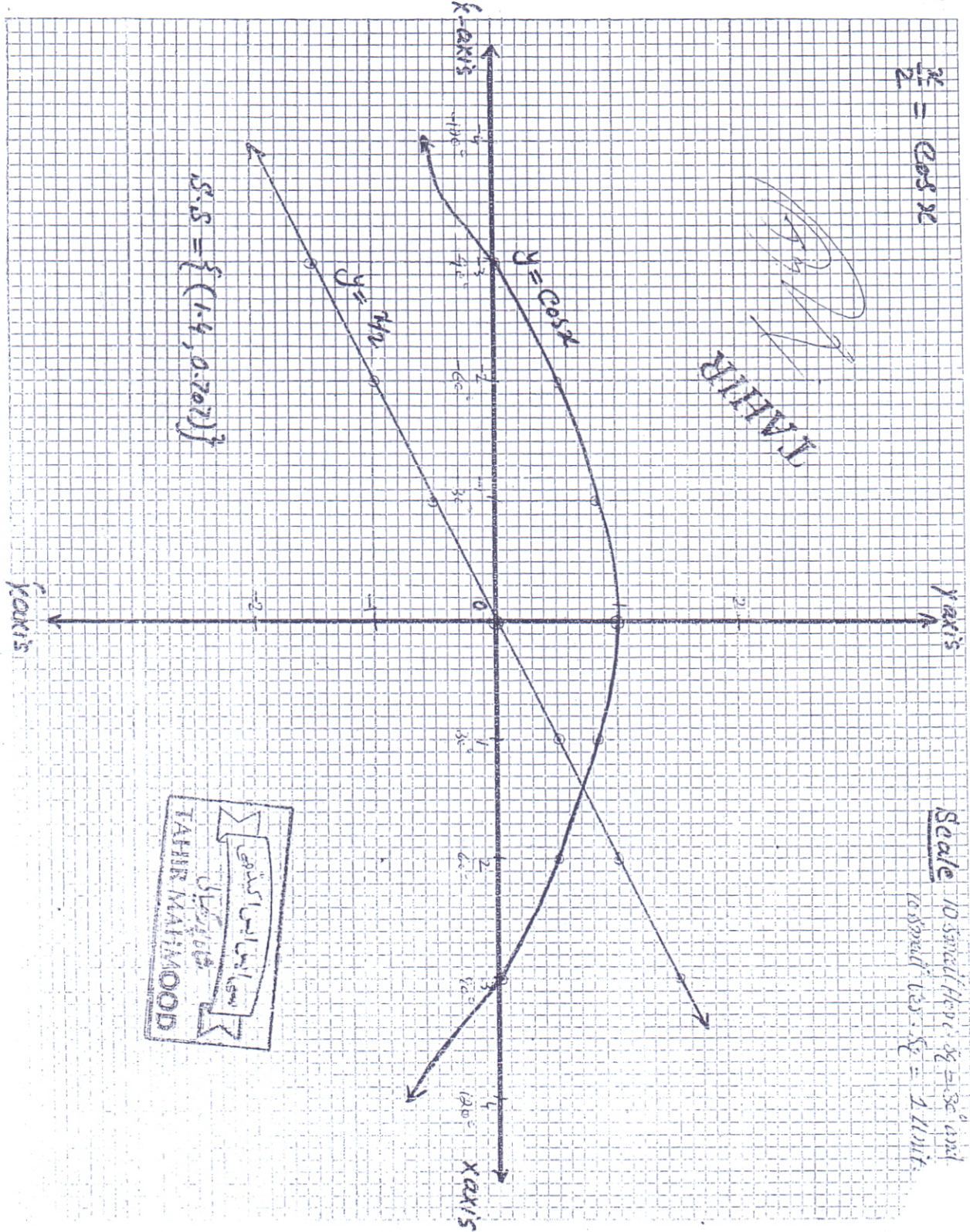


Solution Set
{(0,0)}

(ii)

$\frac{dy}{dx} = \cos x$

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S.S = $\{(1.4, 0.707)\}$

Scale 10 small boxes = 30° and 10 small boxes = 1 unit.

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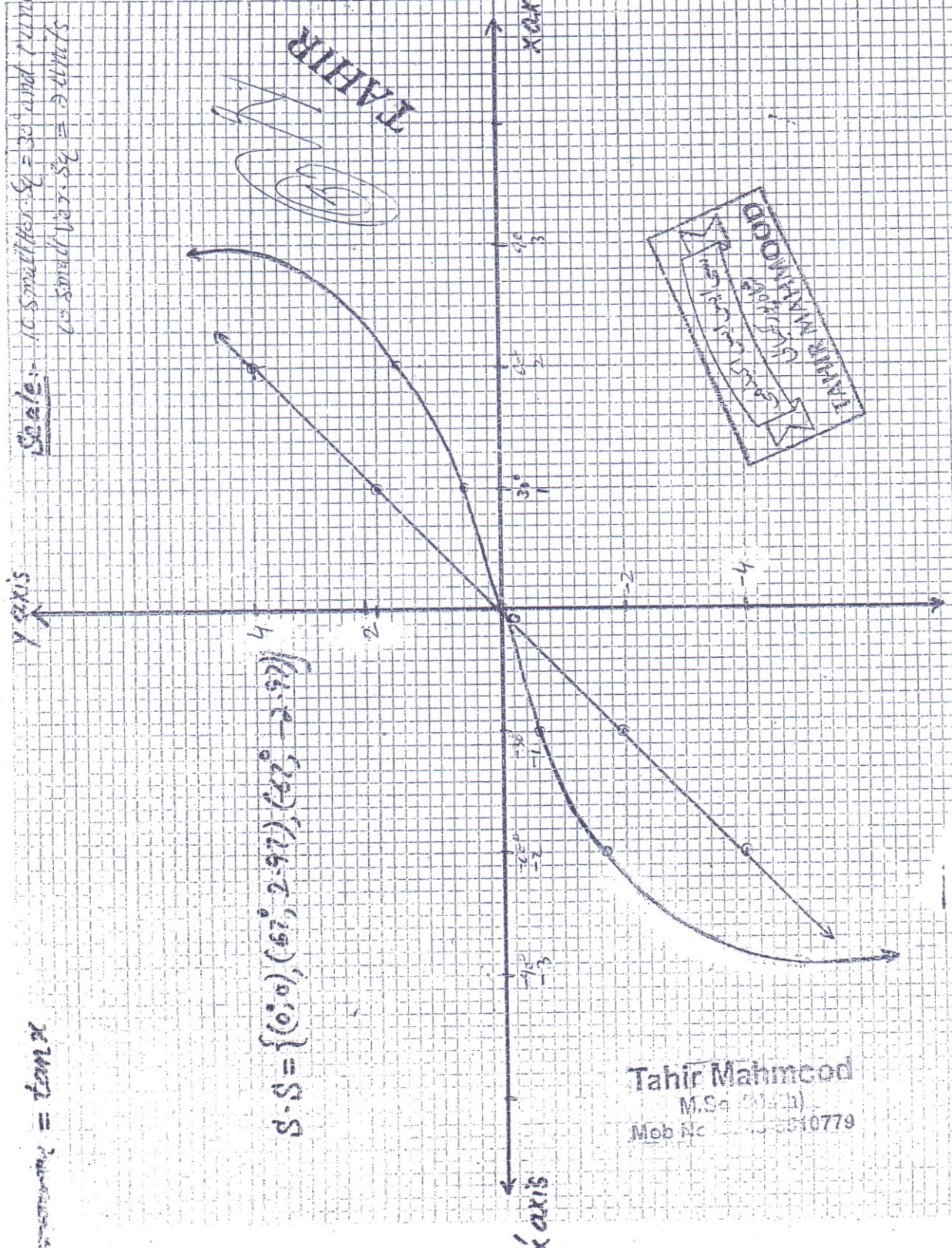
$y = \tan x$

Scale: 10 small squares = 30° and 1 unit

∴ small vertical square = 0.1 units

$S.S = \{(0, 0), (67^\circ, 2.97), (122^\circ, -2.97)\}$

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