DAE/IA-2016/02 SECOND YEAR

(Common with Architecture, Automation, Auto-Mobile & Diesel, Auto & Farm Machinery, Civil, Cast Metal & Foundry, Foundry & Pattern Making, Land & Mine Surveying, Mechanical, Mining, Mechatronics, Metallurgy & Welding, Q. Surveying, Construction Machinery and Footwear Technologies.)

MATH-212 APPLIED MATHEMATICS - II PART - B

Time: 2:30 hours

SECTION - I

Q.1: Write short answer to any Twenty-Five (25) of the following questions: -

 $25 \times 2 = 50$

Marks:80

1	If $f(x) = 3x^2 - 7x + 4$, then find $f\left(\frac{1}{x}\right)$	2	Determine the function, $f(x) = 4x^2 - 7x + 6$ even, odd or neither
3	Evaluate the limit: $\lim_{x \to 3} \sqrt{25 - x^2}$	4	Evaluate the limit $\lim_{x \to 0} \frac{1 - \sin x}{\cos^2 x}$
5	If $y = x^3 + x^2 + 2x + 3$, find $\frac{dy}{dx}$	6	Differentiate $\frac{1}{\sqrt{a^2 - x^2}}$
7	Find $\frac{dy}{dx}$ at the given point if:	8	Find $\frac{dy}{dx}$ if $x^3 + y^3 + 4 = 0$
	$y = x^{2/3}$ at x = 8	_ea	n Ma
9	Differentiate $x^3 + 8$ w.r.t. $x^2 + 4$	10	Find the value of $x \cot x$ w.r.t. 'x'.
11	Find the value of $\frac{d}{dx} (\sin^{-1}x + \cos^{-1}x)$	12	Find $\frac{d}{dx}(a^{x^2})$
13	Find the derivative of $\logigl(\cos^2 xigr)$	14	Find $\frac{dy}{dx}$ when x = a sint, y = cosat
15	If $y = \ell n x$, find y_2	16	Find the turning point of the curve $y = x^2 - 3x + 3$
17	Find $\int \left(x + \frac{1}{x}\right)^2 dx$	18	Evaluate $\int (e^{3x} + e^{5x}) dx$
19	Evaluate $\int \frac{\sin 2x}{\sin x} dx$	20	$Integrate \int \frac{-2x}{\sqrt{4-x^2}} dx$
21	Integrate $\int \frac{dx}{x \ln x}$	22	Integrate ∫sin² x dx
23	Evaluate $\int \frac{dx}{16+9x^2}$	24	Evaluate ∫x e ^x dx
25	Evaluate $\int_{1}^{3} \frac{1}{x+1} dx$	26	Evaluate $\int_0^1 \frac{1}{\sqrt{1-x^2}} dx$
27	$Calculate \int_{0}^{\frac{\pi}{4}} \frac{\mathrm{dx}}{\cos^{2} x}$	28	Write distance formula between two points.
29	Find the coordinates of the mid-point of $P_1(3, 7), P_2(-2, 3).$	30	Find the coordinates of the point P which divide the segment P ₁ (-2, 5) and P ₂ (4, -1) of the ratio of $ \overline{AB} = \sqrt{(2-0)^2 + (3+1)^2}$
31	Reduce the equation $3x + 4y - 2 = 0$ into intercept form.	32	Find the distance from the point $\left(-2,\ 1 ight)$ to the line 3x+4y-12=0
33	Find the equation of the line passing through the point $(-2, 3)$ and having slope $-\frac{1}{2}$.	34	Find the equation of a line through the points $(-1, 2)$ & $(3, 4)$
35	Define Point Circle.	36	Write the equation of circle with, center at $ig({f h}\;,\;{f k}ig)$ and radius ${f r}\;.$
37	Find the radius of the circle $x^2 + y^2 - 4x + y - 1 = 0$		

 $3 \times 10 = 30$

SECTION - II

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Note: ATTEMPT ANY THREE QUESTIONS.

Q.2: (a) Show that $\frac{e^x + 1}{e^x - 1}$ is an odd function of x.

(b) Find the derivative
$$\sqrt{\frac{1+x}{1-x}}$$
 w.r.t 'x'

- Q.3: (a) Find the derivative of $\sin^2 x \cos^3 x$ w.r.t 'x'
 - (b) Find the maximum and minimum values of the function $x^2 4x 6$

dx

 $\sqrt{\mathbf{x}}$

Q.4: (a) Integrate
$$\int \frac{1}{\sqrt{1+x}}$$

(b) Find
$$\int \cos^3 x \, dx$$

Q.5: (a) Evaluate
$$\int x^2 e^x dx$$

- (b) Find the point which is $\frac{7}{10}$ of the way from the point (4, 5) to the point (-6, 10)
- Q.6: (a) A line is parallel to the line 2x + 3y = 5 and passes through (-1, 3). Find an equation for the line.
 - (b) Find which of the two circles $x^2 + y^2 3x + 4y = 0$ and $x^2 + y^2 6x 8y = 0$ is greater.