

**MATH-113 APPLIED MATHEMATICS – I**

COMMON WITH AUTO-MOBILE & DIESEL, AUTO & FARM MACHINERY,  
AUTOMATION, ARCHITECTURE, CAST METAL & FOUNDRY, CHEMICAL,  
CIVIL, CMT, DIE & MOULD, FOUNDRY & PATTERN MAKING, FOOTWEAR, GLASS & CERAMICS  
HEAT VENTILATION, AIR CONDITIONING & REFRIGERATION, LEATHER,  
LAND & MINE SURVEYING, MINING, MECHANICAL, METALLURGY & WELDING,  
MECHATRONICS, PRECISION MECHANICAL & INSTRUMENT, PGA, PETROLEUM,  
PETROCHEMICAL, QUANTITY SURVEY, RAC, SUGAR, TEXTILE SPINNING, TEXTILE DYEING &  
PRINTING & TEXTILE WEAVING TECHNOLOGIES.

**PAPER 'B' (Subjective)**

Time: 2:30 Hours

**SECTION – I**

Marks: 60

Q.1: Write short answer to any Eighteen (18) questions: -

18 × 2 = 36

- Find the magnitude of the vector  $\vec{a} = 2i - 4j + 3k$
- Find a unit vector parallel to the sum of the vectors:  $\vec{a} = [2, 4, -5]$ ,  $\vec{b} = [1, 2, 3]$
- Find a vector whose magnitude is 2 and is parallel to  $5i + 3j + 2k$
- Show that the vectors  $\vec{a} = 3i - j + 7k$ ,  $\vec{b} = -6i + 3j + 3k$  perpendicular to each other.
- Find the area of parallelogram with adjacent sides,  $\vec{a} = 7i - j + k$ ,  $\vec{b} = 2j - 3k$ .
- Define symmetric matrix.
- Show that  $A = \begin{bmatrix} 2 & 3 & -1 \\ 1 & 1 & 0 \\ 2 & -3 & 5 \end{bmatrix}$  is a singular matrix.
- Find x and y if  $\begin{bmatrix} 2 & 1 \\ -3 & 2 \end{bmatrix} = \begin{bmatrix} x+3 & 1 \\ -3 & 3y-4 \end{bmatrix}$
- Without expansion verify that  $\begin{vmatrix} \alpha & \beta + \gamma & 1 \\ \beta & \gamma + \alpha & 1 \\ \gamma & \alpha + \beta & 1 \end{vmatrix} = 0$
- Find  $A^{-1}$  if  $A = \begin{bmatrix} 5 & 3 \\ 1 & 1 \end{bmatrix}$
- Define Isosceles triangles.
- Find the area of a triangle whose two adjacent sides are 16cm and 12cm and their included angle is  $30^\circ$ .
- Define inscribed polygon (circumscribed circle).
- Find the area of regular hexagon circumscribed about a circle of radius 2cm.
- A path 14cm wide, surrounds a circular lawn whose diameter is 360cm. Find the area of the path.
- Find the area of a segment the chord of which 8cm with a height of 2cm.
- Find the area of cross-section of river along a line where the depths at equal interval of 10m are noted 0, 7, 11, 15, 0 meters respectively.
- If the perimeter of a square is 40cm. Find the area of the square.
- Find the area of the whole surface of a right triangular prism whose height is 36m and the sides of whose base are 51, 37 and 20m.
- A brick measures 18cm by 9cm by 6cm. Find the number of bricks that will be needed to build a wall 450cm wide, 18cm thick and 360cm high.
- The cylinder of an air compressor is required to have a working volume of 5 cu. m. if the radius is  $5/6$ m, what must be the stroke.
- The diameter of the base of a right circular cylinder is 14cm and its height is 10cm. Find the volume and surface area of solid cylinder.
- Find the volume of a pyramid whose base is an equilateral triangle of side 1m and whose height is 4m.
- A square pyramid has a volume 60 cu.cm and the side of the base is 6cm. Find the height of the pyramid.
- The circumference of base of a 9m high conical tent is 44 m. Find the volume of the air contained in it.
- Find the cost of painting @ Rs. 7.5 per sq. cm a conical spire 64cm in circumference at the base and 108cm in slant height.
- A spherical cannon ball, 6cm in diameter is melted and cast into a conical mould, the base of which is 12cm in diameter. Find the height of the cone.

SECTION - II

Note: Attempt any three (03) questions.

3 × 8 = 24

- Q.2: From a point within an equilateral triangle perpendicular are drawn to the three sides are 6, 7 and 8 cm respectively. Find the area of triangle.
- Q.3: Find the area enclosed by the curve  $y = 6x - x^2$  and the positive x-axis and y-axis by Simpson's Rule.
- Q.4: A pyramid on a square base has every edge 100m long. Find the edge of a cube of equal volume.
- Q.5: (a) Find the vector whose magnitude is 5 and which is in the direction of the vector  $4i - 3j + k$  ?
- (b) Find the sine of the angle between the vectors  $\vec{a} = i + j + k$  and  $\vec{b} = 2i + 3j - k$
- Q.6: Use Cramer's rule to solve the system of equations: 
$$\begin{cases} x - 2y + z = -1 \\ x + z = 2 \\ -2x + 3y = 5 \end{cases}$$